

## Edge states in two dimensional spin and bosonic systems

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Topological insulators (TIs) [1] have been of great interest in condensed matter physics. One of the most important point is that TIs are characterized by non-local quantities such as topological quantities of the bulk or gapless surface states [2,3]. The TI phases and the surface states are quite stable for any time-reversal symmetric perturbations. On the other hand, the Haldane-gap state in quantum spin systems is another class of the topological state [4], because, similarly to TIs, this gapped state has no local order and is characterized by the non-local (string) order parameter or free spins at the edges. In recent theoretical progress, characteristics of the Haldane-gap state have been captured from the aspect of symmetry and entanglement spectrum [5, 6]. In this study, motivated by the recent development of theories for topological phases and surface states, we study properties of edge states in two-dimensional quantum spin systems and bosonic lattice systems with confinement potential by applying the quantum Monte Carlo method. Focusing on the experimental realization, we particularly focus on the three points; (1) which systems can have gapless edge states, (2) the stability against perturbations, and (3) the difference between the edge modes of TIs and spin systems.

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